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08 July 2020

Version of attached file:

Published Version

Peer-review status of attached file:

Peer-reviewed

Citation for published item:

Ballett, Peter and Hostert, Matheus and Pascoli, Silvia (2020) 'Dark neutrinos and a three-portal connection to the standard model.', *Physical review D.*, 101 (11). p. 115025.

Further information on publisher's website:

<https://doi.org/10.1103/PhysRevD.101.115025>

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Dark neutrinos and a three-portal connection to the standard model

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(Received 27 March 2019; revised manuscript received 24 March 2020; accepted 2 June 2020; published 19 June 2020)

We introduce a dark neutrino sector which respects a hidden $U(1)'$ gauge symmetry, subsequently broken by the vacuum expectation value of a dark scalar. The model is a self-consistent realization of an extended hidden sector that communicates with the standard model only via the three renormalizable portals, namely, neutrino, vector and scalar mixing. The interplay between portal couplings leads to several novel signatures in heavy neutrino, dark photon, and dark scalar searches, typically characterized by multileptons plus missing energy and displaced vertices. A striking signature arises in kaon factories such as NA62, where $K^+ \rightarrow \ell_a^+ \nu \ell_b^+ \ell_c^-$ decays could reveal a heavy neutrino and a light dark photon resonance above backgrounds. Given the open parameter space, we also comment on recent ideas to explain outstanding experimental anomalies, and how they would fit into our proposed model. A minimal extension of the model, possibly motivated by anomaly cancellation, can accommodate a dark matter candidate strongly connected to the neutrino sector.

DOI: [10.1103/PhysRevD.101.115025](https://doi.org/10.1103/PhysRevD.101.115025)

I. INTRODUCTION

The most important evidence that the standard model (SM) of particle physics is incomplete comprises neutrino masses and mixing, and the presence of dark matter (DM) in the Universe. Both call for extensions of the SM and the possible existence of dark sectors which do not partake in SM interactions, or do so with extremely weak couplings while displaying strong “dark” interactions [1–3]. Such sectors might exist at relatively light scales below the electroweak one, being within reach of present and future noncollider experiments. Generically, a neutral dark sector can communicate with the SM via three renormalizable portals. New neutral fermions mix with light neutrinos unless a symmetry differentiates the two, a possibility usually denoted as the neutrino portal. New vector particles can kinetically mix with the SM hypercharge, and new scalars mix with the Higgs boson through the so-called vector and scalar portals, respectively. The latter terms are

generically allowed in the Lagrangian and an explanation of their smallness requires specific UV completions.

In this article, we propose a new neutrino model with a hidden $U(1)'$ gauge symmetry under which no SM fields are charged. We introduce new SM-neutral fermions ν_D and an additional sterile neutrino N . The symmetry is subsequently broken by the vacuum expectation value (VEV) of a complex dark scalar Φ , which gives mass to the new gauge boson. For concreteness, we restrict the scale of the breaking to be below the electroweak one.

Models with heavy neutrinos which are not completely sterile and might participate in new gauge interactions have been studied in several contexts, including $B - L$, $L_\mu - L_\tau$, and left-right symmetric models [4–12], but here we focus on the possibility of a symmetry under which no SM fields are charged [13–17]. New heavy neutral fermions that feel such hidden forces, such as ν_D , are referred to as *dark neutrinos*, since they define a dark sector separate from the SM. Nevertheless, the dark interactions “leak” into the SM sector via neutrino mixing, where they may dominate [18,19]. Models of this type have been invoked to generate large neutrino nonstandard interactions [20,21], generate new signals in DM experiments [18,22–25], weaken cosmological and terrestrial bounds on eV-scale sterile neutrinos [26–33], and as a potential explanation of anomalous short-baseline results at the MiniBooNE [34,35] and/or LSND [36,37]

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experiments with new degrees of freedom at the MeV/GeV scale [38–44].

Our model presents all the three renormalizable portals to the SM in a self-consistent way (see Fig. 1). The Yukawa interactions between the leptonic doublet and N , and between N and ν_D induce neutrino mixing. The gauge symmetry allows a cross-coupling term in the potential between the Higgs and the real part of the scalar, inducing mixing between the two after symmetry breaking. The broken gauge symmetry implies the existence of a light hidden gauge boson X_μ , which mediates the dark neutrino interactions and generically kinetically mixes with the SM hypercharge. This self-consistent setup combines the three portals into a unified picture that exhibits significantly different phenomenology with respect to each portal taken separately. Of particular interest is the fact that the different portal degrees of freedom display novel decay channels and scattering properties, and in many cases would have escaped experimental searches performed to date. We provide a selective list of the most affected bounds, and highlight the most interesting novel signatures that arise. In particular, we propose a new experimental search for the simultaneous presence of heavy neutrino and vector resonances in rare leptonic meson decays. In view of the relatively unexplored parameter space of our model, we comment on how these particles can explain long-standing experimental anomalies. We focus on a novel explanation of the MiniBooNE anomaly, based on the discussion of Ref. [42] (see also Refs. [43,44]), where new neutrino scattering signatures arise at neutrino experiments. We also reconsider the possibility to explain the discrepancy between the prediction [45–49] and measurement [50] of the anomalous magnetic moment of the muon (Δa_μ) via kinetic mixing [51,52]. Finally, we comment on how a scalar that couples strongly to dark neutrinos can help explain the anomalous $K_L \rightarrow \pi^0 \nu \bar{\nu}$ events at KOTO [53].

An interesting feature of the model is the generation of neutrino masses at loop level. This requires only two key features of our setup, namely, a light Z' and neutrino mixing, but not the vector and scalar portals. For this reason, we discuss it elsewhere [54].

In its minimal form, the model is not anomaly free. We discuss how this can be cured and propose a minor extension that introduces additional dark sector neutral fermions charged under the new symmetry [1,2]. Neutrinos, we argue, may be a window into such dark sectors, bridging the puzzles of neutrino masses and DM [55–65]. We briefly outline the key features of a DM extension and leave a more detailed analysis to future work.

II. THE MODEL

We extend the SM gauge group with a new Abelian gauge symmetry $U(1)'$ with associated mediator X_μ and introduce three new singlets of the SM gauge group: a complex scalar Φ , and two left-handed fermions $\nu_{D,L} \equiv \nu_D$

and $N_L \equiv N$. The scalar Φ and the fermion ν_D are equally charged under the new symmetry, and N is neutral with respect to all gauge symmetries of the model. For simplicity, we restrict our discussion to a single generation of hidden fermions. The relevant terms in the gauge-invariant Lagrangian are

$$\begin{aligned} \mathcal{L} \supset & (D_\mu \Phi)^\dagger (D^\mu \Phi) - V(\Phi, H) \\ & - \frac{1}{4} X^{\mu\nu} X_{\mu\nu} + \bar{N} i \not{\partial} N + \bar{\nu}_D i \not{D} \nu_D \\ & - \left[y_\nu^\alpha (\bar{L}_\alpha \cdot \tilde{H}) N^c + \frac{\mu'}{2} \bar{N} N^c + y_N \bar{N} \nu_D^c \Phi + \text{H.c.} \right], \quad (1) \end{aligned}$$

where $X^{\mu\nu}$ is the field-strength tensor for X_μ , $D_\mu \equiv (\partial_\mu - ig' X_\mu)$ is the covariant derivative, $L_\alpha \equiv (\nu_\alpha^T, \ell_\alpha^T)^T$ is the SM leptonic doublet of flavor $\alpha = e, \mu, \tau$, and $\tilde{H} \equiv i\sigma_2 H^*$ is the charge conjugate of the SM Higgs doublet. We write y_ν^α for the L_α – N Yukawa coupling, y_N for the ν_D – N one, and μ' for the Majorana mass of N , which is allowed by the SM and the new gauge interaction, although it breaks lepton number by 2 units.

The minimization of the scalar potential $V(\Phi, H)$ causes the neutral component of the fields H and Φ to acquire VEVs v_H and v_φ , respectively. The latter also generates a mass for both the new gauge boson X_μ and the real component of the scalar field φ . Although v_φ is arbitrary, we choose it to be below the electroweak scale, $v_\varphi < v_H$, as we are interested in building a model that is testable at low scales.

A. Neutrino portal

In the neutral fermion sector and after symmetry breaking, two Dirac mass terms are induced with $m_D \equiv y_\nu^\alpha v_H / \sqrt{2}$ and $\Lambda \equiv y_N v_\varphi / \sqrt{2}$. It is useful to consider the form of the neutrino mass matrix in the single-generation case to clarify its main features. For one active neutrino ν_α ($\alpha = e, \mu, \tau$), it reads

$$\mathcal{L}_{\text{mass}} \supset \frac{1}{2} \begin{pmatrix} \bar{\nu}_\alpha & \bar{N} & \bar{\nu}_D \end{pmatrix} \begin{pmatrix} 0 & m_D & 0 \\ m_D & \mu' & \Lambda \\ 0 & \Lambda & 0 \end{pmatrix} \begin{pmatrix} \nu_\alpha^c \\ N^c \\ \nu_D^c \end{pmatrix} + \text{H.c.} \quad (2)$$

The form of this matrix appears in inverse seesaw (ISS) [66,67] and in extended seesaw (ESS) [68,69] models. In fact, it is the same matrix discussed in the so-called minimal ISS [70], with the difference that in our case its structure is a consequence of the hidden symmetry. After diagonalization of the mass matrix, the two heavy neutrinos ν_h (with $h = 4, 5$) acquire masses. Assuming that $m_D \ll \Lambda$, we focus on two interesting limiting cases.

In the *ISS-like* limit, where $\Lambda \gg \mu'$ and the two heavy neutrinos are nearly degenerate, we have

$$m_5 \simeq -m_4 \simeq \Lambda, \quad m_5 - |m_4| = \mu', \quad U_{\alpha 5} \simeq U_{\alpha 4} \simeq \frac{m_D}{\sqrt{2}\Lambda},$$

$$U_{Di} \simeq \frac{m_D}{\Lambda}, \quad U_{D5} \simeq U_{D4} \simeq \frac{1}{\sqrt{2}}, \quad U_{N5} \simeq U_{N4} \simeq \frac{1}{\sqrt{2}}.$$

In the *ESS-like* case, $\Lambda \ll \mu'$, one heavy neutrino remains very heavy and mainly in the completely neutral direction N , and the other acquires a small mass via the seesaw mechanism in the hidden sector. We find

$$m_4 \simeq -\frac{\Lambda^2}{\mu'}, \quad m_5 \simeq \mu', \quad U_{\alpha 4} \simeq U_{\alpha 5} \sqrt{\frac{m_5}{|m_4|}} \simeq \frac{m_D}{\Lambda},$$

$$U_{Di} \simeq \frac{m_D}{\Lambda}, \quad U_{N5} \simeq U_{D4} \simeq 1, \quad U_{D5} \simeq U_{N4} \simeq \frac{\Lambda}{\mu'}.$$

Note that to lower the scale of the mediators while keeping the heavy neutrino masses large, one must lower the gauge and scalar quartic coupling. Finally, we note that the mixing parameters of ν_4 and ν_5 are correlated in our model. At tree level, the relation

$$\frac{|U_{a5}|^2}{|U_{a4}|^2} = \frac{m_4}{m_5} \quad (3)$$

holds exactly for $a = \alpha, N, D$. Loop corrections are expected to lead to small deviations from this relation. In practice, this implies that ν_4 has typically larger active-heavy mixing than ν_5 .

The Yukawa terms in Eq. (1) induce *neutrino mixing* between the active (light) and heavy (sterile, dark) neutrinos. In this model, similarly to the ISS and ESS cases, this mixing can be much larger than the typical values required in type-I seesaw extensions to explain neutrino masses, making its phenomenology more interesting. The determinant of the mass matrix in Eq. (2) is zero, and so light neutrino masses vanish at tree level and do not constrain the values of the active-heavy mixing angles. This, however, is no longer the case at the one-loop level, as light neutrino masses emerge through radiative corrections from diagrams involving the φ' and Z' particles, as well as SM bosons [54].

B. Scalar portal

In the scalar potential, the symmetries of the model allow us to write down the following term:

$$V(\Phi, H) \supset \lambda_{\Phi H} H^\dagger H |\Phi|^2, \quad (4)$$

where we identify $\lambda_{\Phi H}$ as the scalar portal coupling [71], responsible for mixing in the neutral scalar sector. If such a

term exists, the scalar mass eigenstates (h', φ') mix with the gauge eigenstates (h, φ) as $h' = h \cos \theta - \varphi \sin \theta$ and $\varphi' = h \sin \theta + \varphi \cos \theta$, with a mixing angle θ defined by

$$\tan(2\theta) \equiv \frac{\lambda_{\Phi H} v_H v_\varphi}{\lambda_H v_H^2 - \lambda_\varphi v_\varphi^2}, \quad (5)$$

where λ_H and λ_φ are the quartic couplings of the Higgs and Φ scalars, respectively.

C. Vector portal

Similarly, mixing also arises in the neutral vector boson sector from the allowed kinetic mixing term [72]

$$\mathcal{L} \supset -\frac{\sin \chi}{2} F^{\mu\nu} X_{\mu\nu}, \quad (6)$$

where $F_{\mu\nu}$ is the SM hypercharge field strength. This term may be removed with a field redefinition, resulting in three mass eigenstates (A, Z^0, Z') , corresponding to the photon, Z^0 boson, and the hypothetical Z' boson. For a light Z' , the Z' coupling to SM fermions f to first order in the small parameter χ is given by

$$\mathcal{L} \supset -(eq_f c_W) \chi \bar{f} \gamma^\mu f Z'_\mu, \quad (7)$$

where q_f is the fermion electric charge.

The values of χ and $\lambda_{\Phi H}$ are arbitrary and could be expected to be rather large. As such, we treat them as free parameters within their allowed ranges. Here, we merely note that with our current minimal matter content, χ and $\lambda_{\Phi H}$ receive contributions at loop level from the $(\bar{L}_\alpha \cdot \tilde{H}) N^c$ and $\bar{N} \nu_D^c \Phi$ terms, which are necessarily suppressed by neutrino mixing ($\chi \propto g' e |U_{ah}|^2$ and $\lambda_{\Phi H} \propto |U_{ah}|^2$). These values constitute a lower bound and larger values should be expected in a complete model.

III. DECAY RATES

The phenomenology of the model depends critically on the ordering of the heavy neutrinos and the dark bosons, which controls the decay channels and lifetimes of these particles. In what follows, we list the most relevant decay rates in our model, denoting by ν the combination of all light mass eigenstates (ν_1, ν_2, ν_3) that can appear in a given process. For clarity and simplicity, we separate the light dark boson and heavy dark boson cases, defined by the condition $m_{Z', \varphi'} < m_4$ or $m_4 < m_{Z', \varphi'}$, respectively. We ignore SM contributions to the decay rates, as these are typically subleading for the cases of interest.

A. Heavy bosons

For Z' heavier than the heavy neutrinos, $m_{\nu_h} < m_{Z'}$ with $h = 4, 5$, and with large kinetic mixing, the heavy neutrinos decay predominantly via three-body decays with

an off-shell boson. Unless specified, we assume that the mass of the dark scalar is heavier and does not contribute to the decay rates in this section. The SM Z and Z' contributions can interfere, although we are mainly interested in the case where the latter dominates. The decays of most interest are $\nu_5 \rightarrow \nu_4 \ell^+ \ell^-$ and $\nu_4 \rightarrow \nu \ell^+ \ell^-$, with $\ell = e, \mu$, as far as these channels are kinematically accessible. The decay length of ν_5 critically depends on the mass difference between ν_5 and ν_4 . For concreteness, we focus on specific benchmark points (BPs) that illustrate the key features. In the ISS-like regime, we take $m_4/m_5 = 99\%$ and choose $m_4 \simeq m_5 = 100$ MeV. If χ is negligible, we have that ν_h decays as in the minimal sterile neutrino model case via SM interactions. This is because the $\nu_5 \rightarrow \nu_4 \nu \bar{\nu}$ decay is phase-space suppressed ($\Gamma_{\nu_5 \rightarrow \nu_4 \nu \bar{\nu}} \propto \mu'^5$), and because Z' -mediated decays into three light neutrinos are negligible for small mixing, as $\Gamma_{\nu_h \rightarrow \nu \nu \nu} \propto |U_{ah}|^6 m_{\nu_h}^5/m_{Z'}^4$, where $|U_{ah}|$ is a small mixing parameter between e, μ , and τ flavors with the heavy neutrinos. If χ is sizable, on the other hand, new visible decay channels dominate, specifically $\nu_5 \rightarrow \nu e^+ e^-$ and $\nu_4 \rightarrow \nu e^+ e^-$ for this BP. On the other hand, in an ESS-like regime where $m_4 = m_5/10$, for instance, ν_5 decays into three ν_4 states very rapidly. The subsequent decays of ν_4 would proceed via neutrino and kinetic mixing, but would be much slower than the ν_5 one given the hierarchy of masses and the further suppression due to the portal couplings.

The most relevant decay rate for our case studies is that of heavy neutrinos into a dilepton plus missing energy. Neglecting the electron mass, the decay rate of ν_5 is given by

$$\Gamma(\nu_5 \rightarrow \nu_4 e^+ e^-) \simeq |U_{D5}|^2 |U_{D4}|^2 F(\sqrt{x_4}) \times \frac{(ec_W \chi g')^2 m_5^5}{384\pi^3 m_{Z'}^4}, \quad (8)$$

where $x_4 = m_4^2/m_5^2$ and $F(x) = 1 + 2x - 8x^2 + 18x^3 - 18x^5 + 8x^6 - 2x^7 - x^8 + 24x^3(1-x+x^2)\log x$. Note that $F(0) = 1$ and $F(1) = 0$, with the function obtaining a maximum value of $F(0.09) \simeq 1.09$. For $\sqrt{x_4} = 1 - \epsilon$, one can show that $F(x_4) \rightarrow \epsilon^5$ when $\epsilon \ll 1$, indicating a strong suppression of this decay in ISS-like scenarios, as stated before. Both ν_4 and ν_5 may decay via

$$\Gamma(\nu_h \rightarrow \nu e^+ e^-) \simeq |U_{Dh}|^2 (1 - |U_{D4}|^2 - |U_{D5}|^2) \times \frac{(ec_W \chi g')^2 m_h^5}{384\pi^3 m_{Z'}^4}. \quad (9)$$

For heavier masses, additional decay channels, e.g., $\nu_4 \rightarrow \nu \mu^+ \mu^-$ and $\nu_4 \rightarrow \nu \pi^+ \pi^-$, would become available. A feature of the model is that $\nu_4 \rightarrow \nu \mu^+ \mu^-$ would have the same branching ratio (BR) as the $e^+ e^-$ one, albeit phase space suppressed. Two-body decays into neutral

pseudoscalars via the new force are heavily suppressed due to the vector nature of the gauge coupling, unless mass mixing with the Z is introduced (see Ref. [73] for a thorough discussion of the decay products of a dark photon). Decays into vector mesons are enhanced, where, for instance, we find

$$\Gamma(\nu_h \rightarrow \nu \rho^0) = |U_{Dh}|^2 (1 - |U_{D4}|^2 - |U_{D5}|^2) \times \frac{(ec_W \chi g')^2 m_h^3 f_\rho^2}{16\pi m_{Z'}^4} (1 - r_\rho)^2 \left(\frac{1}{2} + r_\rho\right) \quad (10)$$

for sufficiently heavy dark photons, and where $r_\rho = m_\rho^2/m_h^2$ and $f_\rho \simeq 210$ MeV.

The dominant decays of the heavy dark photon and dark scalar are into heavy neutrinos, and the relevant rates can be obtained from

$$\Gamma(Z' \rightarrow \nu_4 \nu_5) = |U_{D5}|^2 |U_{D4}|^2 \frac{g'^2 m_{Z'}}{12\pi} \times \left(1 + \frac{\Delta r}{2}\right) (1 - R)^{3/2} \sqrt{1 - \Delta r}, \quad (11)$$

where $R = (m_4 + m_5)^2/m_{Z'}^2$ and $\Delta r = (m_5 - m_4)^2/m_{Z'}^2$, and

$$\Gamma(\phi' \rightarrow \nu_4 \nu_5) = |U_{D5} U_{N4} + U_{D4} U_{N5}|^2 \frac{y_N^2 m_{\phi'}}{16\pi} \times (1 - R')^{3/2} \sqrt{1 - \Delta r'}, \quad (12)$$

where $R' = (m_4 + m_5)^2/m_{\phi'}^2$ and $\Delta r' = (m_5 - m_4)^2/m_{\phi'}^2$. Note that as a consequence of $U_{Ni} = 0$ for $i = 1, 2, 3$, the decay $\phi' \rightarrow \nu \bar{\nu}$ vanishes at tree level, and can be neglected here.

B. Light bosons

If $m_{Z'} < m_{\nu_h}$, the heavy neutrino will dominantly and immediately decay as $\nu_h \rightarrow \nu_\alpha Z'$, or even faster for $\nu_5 \rightarrow \nu_4 Z'$ if this is kinematically allowed. For instance, the former decay rate is given by

$$\Gamma(\nu_h \rightarrow \nu Z') = |U_{Dh}|^2 (1 - |U_{D4}|^2 - |U_{D5}|^2) \times \frac{g'^2 m_{\nu_h}^3}{8\pi m_{Z'}^2} (1 - r)^2 \left(\frac{1}{2} + r\right), \quad (13)$$

where $r = m_{Z'}^2/m_{\nu_h}^2$, which agrees with the rate in Ref. [74] under the substitutions $Z' \rightarrow Z$ and $g' \rightarrow g/2c_W$, but differs from the rate in Ref [43]. For (pseudo-)Dirac ν_h , the rate is smaller by a factor of 2. If the scalar is light, $m_{\phi'} < m_{\nu_h}$, decay into the scalar degree of freedom is also possible, with

$$\Gamma(\nu_h \rightarrow \nu\varphi') = |U_{Nh}|^2(1 - |U_{D4}|^2 - |U_{D5}|^2) \times \frac{y_N^2}{16\pi} \frac{m_{\nu_h}^3}{m_{\varphi'}^2} (1-r)^2 \left(\frac{1}{2} + r \right), \quad (14)$$

where $r = m_{Z'}^2/m_{\nu_h}^2$. The Z' subsequently decays into e^+e^- via kinetic mixing with a decay rate

$$\Gamma(Z' \rightarrow \ell^+\ell^-) = \frac{(ec_W\chi)^2}{12\pi} m_{Z'}(1 + 2r_\ell)\sqrt{1 - 4r_\ell}, \quad (15)$$

where $r_\ell = m_\ell^2/m_{Z'}^2$. An analogous expression holds for $\varphi' \rightarrow \ell^+\ell^-$ decays, which are long-lived due to the m_ℓ^2/v_H^2 suppression from the Higgs Yukawa coupling. It is given by

$$\Gamma(\varphi' \rightarrow \ell^+\ell^-) = \frac{\sin^2 \theta_{GF}}{\sqrt{2}} \frac{m_{\varphi'} m_\ell^2}{4\pi} (1 - 4r'_\ell)^{3/2}, \quad (16)$$

where $r'_\ell = m_\ell^2/m_{\varphi'}^2$.

IV. THREE-PORTAL PHENOMENOLOGY

We now present the most relevant signatures arising from the interplay between portal couplings and the heavy neutrinos ($h = 4, 5$). We begin with a discussion of a light dark photon scenario, where we present a novel search for exotic meson decays that can be performed at NA62. Later, we comment on how the usual searches for each particle change with respect to the minimal models, separating our discussion into heavy neutrino, dark photon, and dark scalar searches. For each particle, we then point out how their modified behavior in a three-portal model would fit into recently proposed explanations to outstanding experimental anomalies.

A. Exotic meson decays

From the discussion above, it is clear that if the dark bosons are lighter than the heavy neutrinos, then ν_h decays are fast, and become visible whenever the decays of the light bosons are fast and visible. Because the light scalars typically decay with much longer lifetimes than the dark photons, we will always assume that they lie at much larger masses and do not play a role in our study, unless explicitly stated otherwise. As a proof of principle, we focus on a scenario with a single pseudo-Dirac heavy neutrino ν_h in an ISS-like regime ($\mu' \rightarrow 0$), although it should be noted that in this case neutrino masses vanish. The case of Majorana neutrinos that contribute to light neutrino masses is completely analogous, noting that the mass mechanism is mostly insensitive to small kinetic and scalar mixing parameters. For a comparison with the relevant region for neutrino masses, see Ref. [54].

The most striking signatures associated with the light dark photon scenario arise in kaon factories, where meson decays to heavy neutrinos lead to visible signatures inside

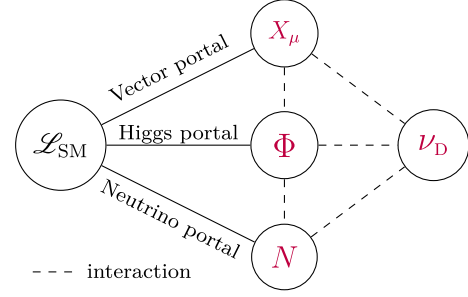


FIG. 1. Schematic representation of our three-portal model.

the detector. In this context, we propose a dedicated search for the following process:

$$M^+ \rightarrow \ell_\alpha^+ \nu_h \rightarrow \ell_\alpha^+ \nu Z' \rightarrow \ell_\alpha^+ \nu \ell_\beta^+ \ell_\beta^-, \quad (17)$$

with $\alpha, \beta \in \{e, \mu\}$ (see Fig. 2). For prompt dark cascades, the BR for such decays is simply $\text{BR}(M^+ \rightarrow \ell_\alpha^+ \nu_h) = |U_{ah}|^2 \rho_\alpha(m_{\nu_h}) \text{BR}(M^+ \rightarrow \ell_\alpha^+ \nu_\alpha)$, where $\rho_\alpha(m_{\nu_h})$ is the Shrock function [75], which accounts for the heavy neutrino mass in such meson decays. This signature can be searched for by applying a simultaneous requirement of

$$m_{\beta\beta}^2 \equiv (p_{\beta^+} + p_{\beta^-})^2 \stackrel{!}{=} m_{Z'}^2, \quad (18)$$

$$m_{p_K - p_\alpha}^2 \equiv (p_K - p_\alpha)^2 \stackrel{!}{=} m_{\nu_h}^2, \quad (19)$$

$$m_{\text{miss}}^2 \equiv (p_K - p_\alpha - p_{\beta^+} - p_{\beta^-})^2 \stackrel{!}{=} 0, \quad (20)$$

within detector resolution. In addition, the strong correlation and smooth distribution over the invariant masses $m_{\alpha\omega}^2 \equiv (p_K - p_{\beta^+} - p_{\beta^-})^2$ and $m_{\alpha\beta\beta}^2 \equiv (p_\alpha + p_{\beta^+} + p_{\beta^-})^2$ can be used to further reduce backgrounds. From kinematics alone, it is possible to show that

$$m_{\alpha\beta\beta}^2 + m_{\alpha\omega}^2 + m_{p_K - p_\alpha}^2 = m_K^2 + m_\alpha^2 + m_{\text{miss}}^2 + m_{\beta\beta}^2, \quad (21)$$

so that a measurement of one can be tested against the other for each point in parameter space.

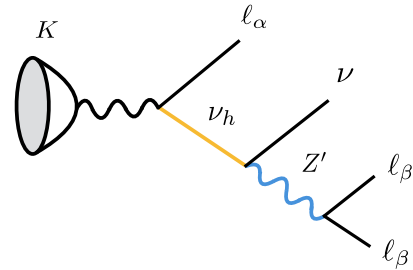


FIG. 2. Kaon decay to a heavy neutrino that decays visibly either through a sequence of two-body decays or via a three-body decay.

Ultimately, the degree of background reduction is highly detector dependent as it arises mainly from resolution and particle identification effects. We return to this issue below, but a detailed analysis is left to the sophisticated detector simulations of the experimental collaborations. We do remark, however, that if the heavy neutral leptons (HNLs) and the dark photon have lifetimes above 10 ps in the rest frame, then they may lead to displaced vertices at NA62, as the boost factors are $\mathcal{O}(100)$ and the resolution for displaced vertices is of $\mathcal{O}(10)$ cm [76]. This provides yet another tool to reduce backgrounds and is particularly useful in the small mixing region where the new physics events are expected to be small. Under the assumption of a light dark photon, a pseudo-Dirac pair that mixes only with the muon flavor, and neglecting final-state masses, the typical lifetimes are

$$\tau_{\nu_h}^0 \simeq 1.7 \text{ ps} \times \left(\frac{10^{-10}}{|U_{Dh}|^2 |U_{\mu h}|^2} \right) \left(\frac{300 \text{ MeV}}{m_{\nu_h}} \right)^3 \quad (22)$$

$$\times \left(\frac{0.375}{g'} \right)^2 \left(\frac{m_{Z'}}{100 \text{ MeV}} \right)^2, \quad (23)$$

$$\tau_{Z'}^0 \simeq 0.70 \text{ ps} \times \left(\frac{10^{-4}}{\chi} \right)^2 \left(\frac{50 \text{ MeV}}{m_{Z'}} \right), \quad (24)$$

where we assumed $\text{BR}(\nu_h \rightarrow \nu Z') \simeq 1$ and $\text{BR}(Z' \rightarrow e^+ e^-) \simeq 1$, with the understanding that $(|U_{D4}|^2 + |U_{D5}|^2)(1 - |U_{D4}|^2 - |U_{D5}|^2) = |U_{Dh}|^2 |U_{\mu h}|^2$ as $\mu' \rightarrow 0$.

In what follows, we obtain an estimate of the single event sensitivity of NA62, assuming a zero-background search. We do this exercise for only 30% of the collected data set corresponding to the period between 2016 and 2018 [77]. Using N_K useful kaon decays, downscaled by a trigger factor to yield N_K^{Fid} fiducial kaon decays, and a detector acceptance A_β , we can find the experimental single event sensitivity to muon-heavy neutrino mixing in $K^+ \rightarrow \mu^+ \nu \ell_\beta \ell_\beta$ decays as

$$|U_{\mu h}|^2 = \frac{1}{N_K^{\text{Fid}} A_\beta \text{BR}(K \rightarrow \mu \nu_\mu)} \frac{1}{P_{\text{dec}}}, \quad (25)$$

where

$$P_{\text{dec}} \simeq (1 - e^{-\frac{\langle L \rangle}{\tau_{\nu_h}^0}}) \text{BR}(\nu_h \rightarrow \nu Z') \times (1 - e^{-\frac{\langle L \rangle}{\tau_{Z'}^0}}) \text{BR}(Z' \rightarrow \ell_\beta \ell_\beta) \quad (26)$$

is a crude approximation for the probability for ν_h and Z' to decay within the average distance between their production and the end of the detector, $\langle L \rangle$, when they have a decay length L_P in the laboratory frame. For concreteness, we take $\langle L \rangle = 37.5$ m. At NA62, $\beta = e$ events ought to be registered by the “dielectron” trigger and $\beta = \mu$ by the “dimuon” trigger [77], each collecting only a fraction of the

TABLE I. Assumptions used for the computation of NA62 single event sensitivity for heavy neutrinos decaying via two-body cascades into two charged leptons plus missing energy.

	$K^+ \rightarrow \mu^+ \nu e^+ e^-$	$K^+ \rightarrow \mu^+ \nu \mu^+ \mu^-$
N_K^{Fid}	2.14×10^{11}	7.94×10^{11}
A_β	4%	10%

total useful kaon decays, and corresponding to a given N_K^{Fid} kaon decays in the fiducial volume, as shown in Table I. We assume a constant acceptance A_β for each final state that is approximately the one obtained in searches for $K^+ \rightarrow \pi^- \ell_\beta^+ \ell_\beta^+$ [77] and $K^+ \rightarrow \pi^+ (\pi^0 \rightarrow \gamma (Z' \rightarrow e^+ e^-))$ [78] at NA62, also shown in Table I.

Our results are shown in Fig. 3. It is clear that within our assumption of no backgrounds, NA62 can probe a large region of unexplored parameter space. Of most relevance is the region at low $m_{Z'}$, where other bounds are rather weak. Incidentally, the dielectron search would directly test the model proposed in Ref. [43] (see MiniBooNE discussion below), where a more phenomenological model with a single heavy neutrino was used. There, all dark couplings are fixed to be large, with $|U_{\mu 4}|^2 \gtrsim 10^{-9}$ and $m_4 \gtrsim 30$ MeV. Fixing g' to be $\mathcal{O}(1)$ implies that heavy neutrinos decay even faster, and the sensitivity curve in Fig. 3 would apply as shown. In our figure, however, we choose to fix v_ϕ so that g' must vary if $m_{Z'}$ varies. If one were to fix g' , only the upscattering cross section region in the plot would be affected, as the cross sections are proportional to $(g' e \chi)^2 |U_{\mu h}^* U_{Dh}|^2$.

We do not study this case here, but $K^+ \rightarrow e^+ \nu \ell_\beta^+ \ell_\alpha^-$ can also be searched for, and would lead to bounds on the $|U_{eh}|^2$ mixing angle, which for promptly decaying Dirac neutrinos is also weakly constrained. Much heavier Z' particles imply that heavy neutrino decay is a three-body process, and may not be so prompt. In that case, the resonance in $m_{\beta\beta}$ is no longer present, making background reduction more challenging. A peak search in $m_{p_K-p_\alpha}^2$ can still be performed, together with the requirement that the invariant masses measured obey Eq. (21), which is still valid. The lifetimes of ν_h in the ISS-like regime of our model are too long to realize this signature, but in an ESS-like regime, $\nu_5 \rightarrow \nu_4 \ell_\beta^+ \ell_\beta^-$ decays are sufficiently fast.

1. Backgrounds

We now discuss backgrounds to our proposed search. An irreducible but smooth background from SM radiative decays $M^+ \rightarrow \ell_\alpha^+ \nu \ell_\beta^+ \ell_\beta^-$ exists at a BR of $\mathcal{O}(10^{-8})$, also displaying $m_{\text{miss}}^2 = 0$. Our signal, however, constitutes a single peak in the $m_{\beta\beta}$ vs $m_{p_K-p_\alpha}$ plane. Given that NA62 has already achieved an invariant mass resolution of $\delta m_{p_K-p_\alpha} = 1\text{--}20$ MeV [81], depending on $m_{p_K-p_\alpha}$, and

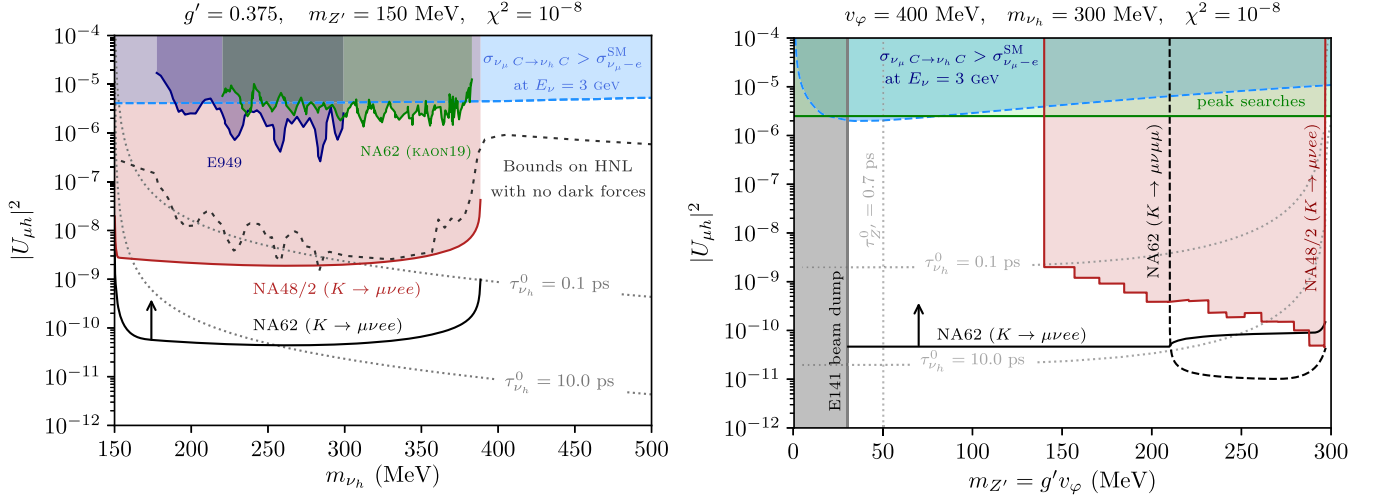


FIG. 3. Parameter space in a phenomenological ISS scenario ($\mu' \rightarrow 0$) where a pseudo-Dirac pair decays visibly via $\nu_h \rightarrow \nu Z' \rightarrow \nu e^+ e^-$. On the left we fix $m_{Z'}$ and vary m_{ν_h} , while on the right we fix m_{ν_h} and vary $m_{Z'}$. The NA62 single event sensitivities to $K^+ \rightarrow \mu^+ e^+ e^- \nu$ and $K^+ \rightarrow \mu^+ \mu^+ \mu^- \nu$ are shown as solid and dashed black lines, respectively. The resonances in $m_{\ell\ell} = m_{Z'}$ and $m_{p_{K-p_\mu}} = m_{\nu_h}$ are expected to greatly reduce backgrounds, although the region $m_{ee} < 140$ MeV can still be challenging due to the large number of π^0 Dalitz decays. We show bounds obtained from the NA48/2 measurement of the rare leptonic kaon decay $K^+ \rightarrow \mu\nu e^+ e^-$ in red [79]. Peak-search constraints on ν_h become less effective due to the fast visible decays, and we rescale these assuming a conservative 0.5% $e^+ e^-$ detection inefficiency. We show the region where the upscattering cross section is larger than that of neutrino-electron scattering in light blue, implying that $e^+ e^-$ pairs could be searched for in accelerator neutrino scattering experiments, such as MINERvA [44]. Beam dump constraints on ν_h disappear, but those on a light Z' remain (for $\chi^2 = 10^{-8}$, E141 [80] provides the strongest bound). The dotted grey contours show a fixed total lifetime for ν_h and Z' . For $|U_{\mu h}| > 10^{-4}$, invisible $Z' \rightarrow \nu\bar{\nu}$ decays start to dominate.

that NA48/2 has achieved $\delta m_{ee}/m_{ee} \simeq 1\%$ [82], we expect radiative leptonic kaon decays to not limit the sensitivity once Eq. (21) has been taken into account. For $K^+ \rightarrow \mu^+ \nu e^+ e^-$, the most challenging background appears at $m_{ee} < m_{\pi^0}$, where the large number of $K^+ \rightarrow \mu^+ \nu_\mu (\pi^0 \rightarrow \gamma e^+ e^-)$ decays can spoof our signature due to the soft nature of the photon in the pion Dalitz decay. The BR of such decays to fake our final states can be naively estimated to be around 10^{-8} for the excellent photon rejection at NA62 of $\simeq 10^{-4}$. This, again, can be further reduced by enforcing invariant mass peaks and correlations. Similar considerations apply for any channel with Dalitz decays. Other backgrounds from $K^+ \rightarrow (\pi^+ \rightarrow \mu^+ \nu) e^+ e^-$, for instance, may be reduced with a cut on $m_{\mu\nu} > m_{\pi^+}$, at the cost of reducing signal acceptance. While our assumption of no backgrounds is optimistic at low $m_{Z'}$ values, the region with $m_{Z'} > 140$ MeV has been studied before in the context of rare leptonic kaon decays, and presents more manageable backgrounds. For instance, the NA48/2 Collaboration [79] has performed a measurement of

$$\text{BR}(K^+ \rightarrow \mu^+ \nu e^+ e^-) = (7.81 \pm 0.21 \text{ stat.}) \times 10^{-8} \quad (27)$$

for $m_{ee} > 140$ MeV, where we omitted the smaller systematic uncertainties. This measurement achieved an overall signal-to-background ratio of $\simeq 30$, with an estimate of 54 backgrounds events.

For the dimuon channel, $K^+ \rightarrow \pi^+ \pi^+ \pi^-$ presents the largest background rate, followed by $K^+ \rightarrow \mu^+ \nu \pi^+ \pi^-$. These channels are challenging due to the subsequent decays of the $\pi^\pm \rightarrow \mu^\pm \nu$ as well as the misidentification rate of $\pi \rightleftharpoons \mu$ of 0.4–0.9% at NA62. The radiative leptonic decay $K^+ \rightarrow \mu^+ \nu \mu^+ \mu^-$ would also present a background. No measurement of such SM decays exists but the most stringent limit comes from E787, where it was found that

$$\text{BR}(K^+ \rightarrow \mu^+ \nu \mu^+ \mu^-) < 4.7 \times 10^{-7} \quad (28)$$

at 90% C.L. for $m_{\mu\mu} \in [220, 320]$ MeV [83]. NA62 will measure such SM decays, as shown in Ref. [84] which explored placing constraints on new light $L_\mu - L_\tau$ mediators. In comparison with the latter study, the multiple invariant mass resonances in our model would further reduce backgrounds and offer valuable insight if the light dark photon can decay to muons. A simultaneous detection in the electron and muon channels in accordance with the dark photon BRs would offer strong evidence for our kind of dark sector.

2. Similar measurements

A bound can already be derived from existing measurements compatible with the SM prediction in kaon radiative leptonic decays [79,85,86]. The NA48/2 Collaboration has measured the BR of $K^+ \rightarrow \mu^+ \nu e^+ e^-$ as a function of m_{ee} ,

starting from $m_{ee} > 140$ MeV, and great agreement between Monte Carlo simulations and data is observed [79]. This allows us to set constraints on $m_{Z'} > 140$ MeV, for various values of m_{ν_h} . We show the region where the new physics events are larger than 20% of the measured value for $m_{Z'} = 150$ MeV in the left panel of Fig. 3. The same is done for $m_{\nu_h} = 300$ MeV and varying $m_{Z'}$ in the right panel. Note that for $2m_\mu < m_{Z'}$, one would predict $K^+ \rightarrow \mu^+ \nu \mu^+ \mu^-$ decay, which results in a rather weak limit if compared with the m_{ee} -binned $K^+ \rightarrow \mu^+ \nu e^+ e^-$ measurement at NA48/2.

Finally, similar signatures can arise in pion decays $\pi^+ \rightarrow \ell_\alpha^+ \nu e^+ e^-$. For $\alpha = e$, a measurement compatible with the SM prediction was performed at the SINDRUM magnetic spectrometer [87] where

$$\text{BR}(\pi^+ \rightarrow e^+ \nu e^+ e^-) = (3.4 \pm 0.5) \times 10^{-9}. \quad (29)$$

No measurement or limit exists for $\pi^+ \rightarrow \mu^+ \nu e^+ e^-$, where only $m_{\nu_h} \lesssim 34$ MeV heavy neutrinos can be tested. Productions in muon [88] and tau [89] leptonic decays of the type $\ell_\alpha \rightarrow \ell_\beta \ell_\gamma \ell_\gamma \nu \bar{\nu}$ with BRs of $\mathcal{O}(10^{-5})$ are much less constraining, although tau decays would offer a unique process to test the less constrained $|U_{th}|$ parameter.

B. Impact on heavy neutrino searches

In this subsection and the ones that follow it, we will discuss a collection of interesting signatures and the most relevant changes to the current experimental landscape in a model such ours, where at least two portal couplings may be at play. We do not make the assumption of a pseudo-Dirac HNL anymore, and use ν_h to denote both ν_4 and ν_5 , whenever the distinction is not important. In the presence of only neutrino mixing, the strongest bounds on heavy neutrinos in the MeV–GeV mass range come from peak searches in meson decays [90–92] and beam dump experiments [93–98] looking for visible ν_h decays. As we will see, both searches can be weakened if the ν_h decays are sufficiently different from the case of “standard” sterile neutrinos with SM interactions suppressed by neutrino mixing.

1. Peak searches and LNV

Peak searches in meson decays of the type $M \rightarrow \ell \nu_h$ have long been regarded as model-independent bounds on heavy neutrinos. This is due to the fact that only the parent meson and daughter charged lepton kinematics need to be measured in order to search for a peak in $(p_M - p_\ell)^2 = m_{\nu_h}^2$. We argue that the strict requirement of observing a single charged track in the detector [91] would, however, veto a large fraction of new physics events if ν_h decays promptly into $\nu_\alpha \ell^+ \ell^-$, for instance. This is not a concern in minimal sterile neutrino extensions of the SM due to the large lifetime of ν_h , which is greatly reduced for

large values of χ in our model. We illustrate this effect in the left panel of Fig. 3, where peak search bounds on $|U_{\mu h}|^2$ derived from $K^+ \rightarrow \mu^+ \nu_h$ decays at KEK [90], E949 [91], and NA62 [81,99] are reinterpreted in an ISS-like BP where a single heavy neutrino of Dirac nature undergoes two-body decays into $\nu e^+ e^-$ final states. With a probability to miss an $e^+ e^-$ pair in the preceding detectors of 0.5%, this represents a 200 times weaker bound on the mixing angle. This inefficiency is clearly a conservative assumption based on the *photon* detection inefficiency (typically larger than that of an $e^+ e^-$ pair of the same energy) reported by the E949 [91] and NA62 [100] collaborations. In addition, bounds on lepton number violation (LNV) from meson and tau decays are affected [74,101]. These bounds are obtained by searching for $M^+ \rightarrow \ell^+ \nu_h \rightarrow \ell^+ \ell^+ \pi^-$ decays, with the same-sign dileptons being a smoking gun for LNV by two units. In our current model, the intermediate on-shell ν_h produced in said decays has very suppressed charged-current branching ratios into $\ell^\pm \pi^\mp$ and $\ell^\pm K^\mp$ final states, and so such bounds are much weaker.

2. Beam dump searches

Beam dump and fixed target experiments are an ideal place to search for heavy neutrinos due to the large number of meson decays involved. The search strategy is based on producing such particles in decays at the target, and searching for their visible decay products in a detector located at a fixed distance from the target. If heavy neutrinos decay into visible particles faster than in the minimal sterile neutrino model, then such constraints on the mixing angle of heavy neutrinos are affected. As shown in Ref. [102], if one only enhances the decay $\Gamma(\nu_h \rightarrow \nu e e)$ by a factor α with respect to its value in the minimal sterile model, then the upper bounds become stronger by a factor $\simeq \sqrt{\alpha}$, while the lower bounds become weaker by a factor $\simeq \alpha$. This can be understood by noting that in the vicinity of the upper bound the number of events is proportional to $|U_{ah}|^4$, while near the lower bound it is proportional to $|U_{ah}|^2$, as most particles decay inside the detector. For very short decay lengths, no bound can be placed, as all particles decay before reaching the detector. For this reason, beam dump bounds on ν_5 typically vanish, while those on ν_4 become stronger in an ESS-like regime. This typically introduces problems with searches at PS-191 [93], but can be evaded in nonminimal realizations of our model where the correlation between the mixing parameters of ν_4 and ν_5 is broken. We come back to this issue when discussing MiniBooNE.

C. Exotic neutrino scattering signatures

The presence of a light vector mediator and kinetic mixing can also induce new neutrino scattering signatures. For a hadronic target \mathcal{H} , light neutrinos may upscatter electromagnetically via the Z' into ν_h , which subsequently

decays into observable particles, e.g., $\nu_\alpha \mathcal{H} \rightarrow (\nu_h \rightarrow \nu \ell_\beta^+ \ell_\beta^-) \mathcal{H}$. Beyond offering a novel scenario to explain the MiniBooNE low-energy excess (see below), such upscattering can also produce exotic final states in neutrino detectors such as e^+e^- , $\mu^+\mu^-$, multimeson, and $\tau^+\tau^-$ final states. If $m_{Z'} < m_{\nu_h}$, the on-shell Z' decays can be searched for by looking for neutrino-produced dileptons with $m_{\ell\ell} = m_{Z'}$. Dimuon production, however, is tightly constrained due to kaon decay bounds (see above), unless $m_{\nu_h} \gtrsim 400$ MeV. In that case, signatures from $Z' \rightarrow \pi^+\pi^-$ decays would appear for $2m_\pi < m_{Z'}$ MeV. If $m_{Z'} \lesssim 140$ MeV, neutrino upscattering on nuclei is predominantly coherent, and leads exclusively to e^+e^- final states. These can mimic single-photon showers in neutrino detectors, and could affect sideband measurements in neutrino-electron scattering data at (multi-)GeV energies (see Ref. [44]). Assuming an ISS-like model and a light dark photon, we show the region where the coherent upscattering cross section on carbon ($\nu_\mu C \rightarrow \nu_h C$) is larger than that of neutrino-electron scattering in the SM in Fig. 3. When $m_{Z'} \gtrsim 800$ MeV, upscattering happens predominantly on protons. In that case, more hadronic activity in the detector is expected, and neutrino-electron scattering measurements are no longer as effective. If $2m_\mu < m_{Z'} < m_{\nu_h}$ or $2m_\mu < m_{\nu_h} < m_{Z'}$, then such events contribute to neutrino-trident production ($\nu_\mu \mathcal{H} \rightarrow \nu_\mu \mu^+ \mu^- \mathcal{H}$) at neutrino scattering experiments if ν_h decays fast enough. Previous measurements at CCFR [103] and CHARM-II [104] led to weak bounds in the parameter space shown in Fig. 3, so we do not show them here. They become relevant when $m_{Z'} \gtrsim 800$ MeV as neutrino-electron scattering becomes ineffective.

1. MiniBooNE low-energy excess

The upscattering signatures discussed above with $\ell^\pm = e^\pm$ have been invoked as an explanation of the excess of low-energy electron-like events at MiniBooNE [35] in Refs. [43] and [42], where a simplified model containing a single heavy neutrino was used. This explanation relies on the fact that collimated or highly energy-asymmetric e^+e^- pairs can mimic an electron-like signature in Cherenkov detectors, such as MiniBooNE. While the light dark photon case ($m_{Z'} < m_{\nu_4}$) [43] leads to tension with either the angular distribution at MiniBooNE or $\nu - e$ scattering data [44], the heavy dark photon study ($m_{\nu_4} < m_{Z'}$) [42] finds a good fit to both energy and angular distributions at MiniBooNE, while evading constraints from $\nu - e$ scattering data. The preferred parameters were $m_4 = 140$ MeV, $m_{Z'} = 1.25$ GeV, $g' = 1$, $|U_{\mu 4}|^2 = 1.5 \times 10^{-6}$, and $\chi^2 = 5 \times 10^{-6}$. There, the prompt decays of $\nu_4 \rightarrow \nu e^+e^-$ were achieved by requiring a large mixing with the tau flavor, namely, $|U_{\tau 4}|^2 = 7.8 \times 10^{-4}$. We note, however, that the decay lengths achieved by Ref. [42] are too long when computed using our expressions, and may indicate that much larger values of dark couplings were used than the

ones quoted. In addition, choosing values of $|U_{\tau 4}|^2 = 520 \times |U_{\mu 4}|^2$ or larger would imply that experiments with a large component of ν_τ neutrinos in their beam would see ν_4 production at a comparable rate to their total neutral-current elastic scattering rate. With a similar e^+e^- -electron misidentification invoked to explain the MiniBooNE excess, such events would lead to large numbers of ν_e -like events at the far detector of T2K, in contradiction with ν_e appearance measurements¹ [105].

In an ESS-like limit of our current model, we predict that both ν_4 and ν_5 can be produced in upscattering. Due to the larger $\nu_5 - \nu_4 - Z'$ coupling compared to that of $\nu_4 - \nu_i - Z'$, we can do away with the need for a large $|U_{\tau h}|^2$ mixing by producing sufficient numbers of ν_5 states in the MiniBooNE detector. We take an analogous benchmark point to that of Ref. [42]:

$$\begin{aligned} m_4 &= 80 \text{ MeV}, & m_5 &= 140 \text{ MeV}, \\ |U_{\mu 5}|^2 &= 4/7 \times |U_{\mu 4}|^2 = 1.5 \times 10^{-6}, \\ |U_{D4}|^2 &= 7/4 \times |U_{D5}|^2 = 7/11, \\ g' &= 2, & \chi^2 &= 1 \times 10^{-5}, \quad \text{and} \quad m_{Z'} = 1.25 \text{ GeV}. \end{aligned} \quad (30)$$

For these parameters, we find that ν_4 is very long-lived ($c\tau_4^0 \simeq 30$ km) and its production only introduces a small deviation from the total number of neutral-current events due to $\nu_\mu \mathcal{H} \rightarrow \nu_4 \mathcal{H}$. On the other hand, the signature

$$\nu_\mu \mathcal{H} \rightarrow (\nu_5 \rightarrow \nu_4 e^+ e^-) \mathcal{H} \quad (31)$$

fakes the MiniBooNE signal due to prompt ν_5 decays ($c\tau_5^0 \simeq 76$ cm). Decays of the type $\nu_5 \rightarrow \nu_4 \nu \nu$ are doubly suppressed by the small mixing angles,² and have the second largest BR of $\simeq 8 \times 10^{-5}$. The angular spectrum is analogous to weakly scattering neutrinos due to the large value of $m_{Z'} = 1.25$ GeV, but contains only a vectorial piece coupling to matter. We also expect a larger efficiency to select signal events in our model, as we predict a larger number of events with overlapping showers (defined approximately as $\Delta\theta_{ee} \lesssim 13^\circ$ at MiniBooNE [35], where $\Delta\theta_{ee}$ is the opening angle of the two electrons) as well as events that are highly asymmetric in energy, both being categories that fake single electromagnetic shower events. This is due to the low invariant masses m_{ee} that are now bounded by $m_{ee} < m_5 - m_4 = 60$ MeV, compared with $m_{ee} < m_4 = 140$ MeV in Ref. [42]. For the parameters

¹We thank Pedro Machado for bringing this argument to our attention.

²In fact, even if the intermediate state becomes lighter, say, $m_4 = 50$ MeV, the $\nu_5 \rightarrow \nu_4 \nu_4 \nu$ BR would be comparable to that of $\nu_5 \rightarrow \nu_4 e^+ e^-$. Decays of the type $\nu_5 \rightarrow \nu_4 \nu_4 \nu_{(4)}$ dominate whenever $3m_4 < m_5$.

quoted above, we predict a total number of upscattering events on carbon plus protons in the full MiniBooNE detector of $\simeq 6.3 \times 10^3$ for ν_4 , and $\simeq 6.1 \times 10^3$ for ν_5 , before detection and signal efficiencies. These numbers correspond to 12.84×10^{20} protons on target in neutrino mode for 818 t of CH, and overall efficiencies are expected to be of the order of 5%. We note that our rate differs from that of Ref. [42], and that the source of discrepancy is still unknown but likely to be due to larger dark couplings than the ones quoted by the authors. The upscattering rate via Z' exchange is proportional to $|\sum_i U_{\mu i}^* U_{D i}|^2 = |U_{\mu 4}^* U_{D 4} + U_{\mu 5}^* U_{D 5}|^2$ and for our parameters we find negligible interference with SM bosons.

Beam dump constraints on such an unstable ν_5 particle disappear completely and peak searches are weakened, as discussed above. For ν_4 , the only relevant constraint is that posed by the beam dump experiment PS-191 [93], where production through $K^+ \rightarrow \mu^+ \nu_4$ and decay via the Z' -enhanced channel $\nu_4 \rightarrow \nu e^+ e^-$ would take place. Although the $|U_{\mu 4}|^2$ parameter plays no role in the MiniBooNE explanation, it is heavily correlated with $|U_{\mu 5}|^2$ in our three-neutrino theory. Therefore, we can conclude that our benchmark point is most likely in contradiction with the constraint posed by PS-191 on $|U_{\mu 4}|^2$, unless such correlation is broken. A more quantitative estimate of the tension is challenging as no event selection information was provided in the original PS-191 analysis and since it assumed only charged-current decays of heavy neutrinos. We also note that an excess of electron-like events with additional tracks was later reported and attributed to neutrino interactions inside the detector [106–108] (see also the discussion in Ref. [109]).

Finally, let us emphasize that the parameters chosen in Eq. (30) are within the range of mass and mixings required to explain light neutrino masses. For instance, assuming a 2 GeV scalar, we find that $m_\nu \simeq 0.4$ eV for Eq. (30), according to Eq. (8) of Ref. [54].

D. Impact on dark photon searches

Bounds on the vector portal come from several different sources [110,111]. Electroweak precision data and measurements of the $(g-2)$ of the muon and electron constrain our model [112]. Major efforts at collider and beam dump experiments led to strong constraints on dark photons by searching for the production and decay of these particles. Such bounds, however, depend on the lifetime of the Z' and on its BR into charged particles. In our model, the Z' decays invisibly into heavy fermions if $2m_4 < m_{Z'}$ and into light neutrinos otherwise. In the latter case, constraints would be much weaker than usually quoted when considering only monophoton searches [113]. In the former case, however, new signatures arise, where the subsequent decay of ν_h leads to multilepton/multimeson events, potentially with displaced vertices and providing a very clean experimental

signature. Notably, if the Z' decays into ν_h states that subsequently decay sufficiently fast within the detector, even the “invisible decay” bounds will be weakened.

1. Revisiting Δa_μ

The above possibility opens the option to explain the discrepancy between the theoretical prediction [45–49] and the experimental value [50] of the $(g-2)$ of the muon via kinetic mixing. For instance, a 1 GeV Z' with $\chi = 2.2 \times 10^{-2}$ can explain a_μ . Taking ν_4 around 800 MeV and $m_{Z'} < m_5$, the Z' would decay into $\nu_4 \nu$ immediately. For the quoted value of the kinetic mixing and $|U_{\mu 4}|^2 = 10^{-5}$, for instance, the heavy fermions would predominantly decay with sub-cm decay lengths to $e^+ e^-$ and $\mu^+ \mu^-$ pairs plus missing energy, as well as into $\nu \rho^0$ around 1% of the time. This region of the χ parameter space is constrained only by the BABAR $e^+ e^-$ collider searches for visible [114] and invisible decays [113] of a standard dark photon. Both of these searches would veto the three-body decays of ν_4 , opening up a large region of parameter space (see Refs. [115,116] for a similar discussion in inelastic DM models). Resonance searches still constrain the Z' BR into $e^+ e^-$ and $\mu^+ \mu^-$ which are proportional to χ^2 , providing a weak upper bound. A detailed analysis to identify the viable parameter space will be done elsewhere. Note that neutrino masses are too large for the mixing quoted, but can easily be accommodated by extending the neutral fermion sector.

E. Impact on dark scalar searches

For the scalar portal, the coupling $\lambda_{\Phi H}$ is rather weakly bound by electroweak precision data and the measurement of the Higgs invisible decay at the level of $\lambda_{\Phi H} \lesssim 0.1$ [117]. For processes involving $\lambda_{\Phi H}$, the physical observables are suppressed by mass insertions due to the nature of the Higgs interaction. Nevertheless, ϕ' may decay to a pair of ν_h states and lead to multilepton signatures inherited from ν_h decays, potentially also in the form of displaced vertices. For this reason, bounds on visible decays of ϕ' no longer apply, and the parameter space $(m_{\phi'}, \sin \theta)$ is wide open when $\phi' \rightarrow \nu_h \nu_h \rightarrow \text{visible}$ happens on the cm scale.

1. Unexplained KOTO events

The new scalar decays can be invoked to explain the recent anomalous number of $K_L \rightarrow \pi^0 \nu \bar{\nu}$ events reported by the KOTO Collaboration [53]. In our model, this can be achieved in the range $m_{\phi'} = 120\text{--}170$ MeV and $\theta^2 \simeq 4 \times 10^{-7}$, evading $K^+ \rightarrow \pi^+ \phi'$ searches at NA62 [118] and E949 [119] bounds due to large pion backgrounds at $(p_K - p_\pi)^2 \simeq m_\pi^2$ [120]. In addition, if $\phi' \rightarrow \nu_h \nu$ decays are fast, then two scenarios arise. First, if ν_4 is very long-lived, e.g., $m_5 \gg m_4 = 100$ MeV, $\chi \rightarrow 0$, and $|U_\alpha|^2 \lesssim 10^{-6}$, then beam dump constraints on ϕ' , such as the ones posed by the CHARM experiment [121], are relaxed. Second, if ν_h

is short-lived, then one may invoke the “lifetime gap” explanation proposed in Ref. [122]. In this case, the dark scalar can decay visibly through a dark cascade with

$$c\tau^0(\varphi' \rightarrow \nu_4\nu \rightarrow \nu\nu Z' \rightarrow \nu\nu e^+e^-) \simeq 10 \text{ cm}, \quad (32)$$

and so it is vetoed in the large-acceptance NA62 and E949 detectors [118], but would inevitably count as signal for the smaller KOTO detector. The latter scenario is tightly constrained by beam dump searches at ν Cal [123–125], which, despite their large uncertainties in the region of interest [126], will be mildly alleviated due to the smaller boosts and geometrical acceptance introduced by the dark cascade. This three-portal signature with finite ν_4 lifetime can be achieved for $g' = 0.1$, $\chi \simeq 2 \times 10^{-4}$, $m_{Z'} = 50 \text{ MeV}$, $m_4 = 100 \text{ MeV}$, $|U_{\alpha 4}|^2 \lesssim 10^{-10}$, and $m_{\varphi'} = 140 \text{ MeV}$.

F. Neutrinophilic limit

In the limiting case of a neutrinophilic model ($\chi = \lambda_{\Phi H} = 0$), the vector and scalar particles present a challenge for detection. Nonetheless, if light, they can be searched for in meson decays [127,128] and at neutrino experiments [129]. Finally, the faster decays of ν_h and its self-interactions can help ameliorate tensions with cosmological observations. We do not comment further on this, but note that great effort has been put into accommodating eV-scale sterile neutrinos charged under new forces with cosmological observables [26–31,130] (see also Ref. [131] for an interesting discussion where the Z' decay to neutrinos leads to an altered expansion history of the Universe). We note that an eV sterile neutrino with relatively large mixing could be easily accommodated in our ESS framework. The eV neutrino would be mainly in the ν_D direction and would have strong hidden gauge interactions.

V. DARK MATTER

Given the presence of a dark sector, we can ask if the model can accommodate a DM candidate. This can be achieved by introducing new fermions that do not mix with the neutrinos, in order to preserve their stability. A minimal solution would be to introduce a fermionic field ψ_L which has $U(1)'$ charge $1/2$. The different charges of ψ , ν_D , and N would forbid neutrino mixing. A Majorana mass term

$$\psi_L^T C^\dagger \psi_L \quad (33)$$

would emerge after hidden-symmetry breaking, leading to a Majorana DM candidate. Anomaly cancellation requires additional particle content, such as promoting all charged fermions to vector-like states.

Another realization with additional symmetries can be made anomaly free. Following Ref. [65], we introduce a pair of chiral fermion fields ψ_L and ψ_R , and charge only the latter under the $U(1)'$ symmetry with the same charge as

ν_D . This choice ensures anomaly cancellation, and allows us to write

$$y_\psi \bar{\psi}_L \psi_R \Phi^\dagger, \quad (34)$$

which after hidden-symmetry breaking yields a Dirac mass m_ψ . In general, ψ_L may also have a Majorana mass term μ_ψ , giving rise to a two-component Majorana dark matter sector. Setting $\mu_\psi \rightarrow 0$ is technically natural, and would ensure a Dirac dark matter candidate. In order to avoid $\psi_R - \nu_D$ and $\psi_L - N$ mixing, an additional \mathbb{Z}_2 symmetry may be imposed, under which all particles have charge $+1$, except for ψ_L and ψ_R , which have charge -1 . This so-called dark parity can be thought of as a consequence of lepton number L . Since $L(\psi) = 0$, the Majorana mass term for N is the only soft breaking term, which breaks lepton number by $\Delta L = 2$ units. Lepton number is then reduced to conservation of lepton parity $(-1)^L$, which can then be shown to be equivalent to our dark parity [132].

If the scalar and vector portal couplings are small in such scenarios, DM interacts mainly with neutrinos. Direct-detection bounds are then evaded, since interactions with matter are loop suppressed. Indirect detection, on the other hand, is more promising as DM annihilation into neutrinos would dominate. For instance, take the mass of ψ to be smaller than the masses of the Z' , φ' , and both heavy neutrinos. In this case, the DM annihilation is directly into light neutrinos via $\psi\bar{\psi} \rightarrow \nu_i\nu_i$. This yields a monoenergetic neutrino line that can be looked for in large-volume neutrino [133,134] or direct-detection experiments [25]. Alternatively, if m_ψ is larger than the mass of any of our new particles, then the annihilation may be predominantly into such states via $\psi\bar{\psi} \rightarrow XX$, where $X = \varphi'$, Z' , or ν_h , which subsequently decay to light neutrinos. In this secluded realization [135], the neutrino spectrum from such annihilation is continuous [61], but neutrino-DM interactions are expected to be large and can be searched for in a variety of ways [64,136–139].

VI. CONCLUSIONS

We have proposed a new model which invokes the existence of a hidden $U(1)'$ symmetry confined to a new dark neutrino sector. Without restricting to the region where our model generates the correct neutrino masses, we explored a series of experimental signatures that may arise from the interplay of portal couplings. The simultaneous presence of neutrino, vector kinetic, and scalar mixing in a self-consistent framework allows for a diverse phenomenology. In particular, signatures such as multilepton final states with missing energy, displaced vertices, rare leptonic decays, and unique final states in neutrino scattering processes are a hallmark of such nonminimal models. We have also argued that previously excluded parameter space for the minimal realization of each portal coupling opens up due to faster and semivisible decays in the dark

sector. This also impacts peak searches in meson decays, often regarded as model-independent bounds. For heavy neutrinos that decay to light dark photons, we identified a unique signature at kaon experiments, wherein three charged-lepton final states can be used to search for this class of dark sectors, and in the case of a signal, reveal the heavy neutrino and dark photon masses. This search can be performed at NA62, where significant improvement over current bounds can be achieved. These searches are particularly relevant at low dilepton invariant masses m_{ee} , as they could further test the phenomenological model discussed in Refs. [43,44], where low-energy dielectrons produced in neutrino upscattering explain the energy distribution of the MiniBooNE excess.

The model also offers exciting new avenues to explain currently outstanding experimental anomalies. In this article, we discussed how recently proposed explanations would fit within a nonminimal dark sector like ours, each with their separate choice of parameters. For the MiniBooNE low-energy excess, we proposed a GeV-scale Z' for the angular distribution, and a pair of heavy neutrinos with $m_4 \simeq 80$ MeV and $m_5 \simeq 140$ MeV. The decays of ν_5 are cm scale, but ν_4 travels much longer distances. Unfortunately, such ν_4 particles have enhanced lifetimes with respect to the minimal model, and are in tension with the PS-191 beam dump experiment unless the correlation present in the three-neutrino model between the ν_4 and ν_5 mixing angles is broken. For heavy neutrinos with a larger mass $m_4 \simeq 800$ MeV, a Z' of 1 GeV with $\chi = 2.2 \times 10^{-2}$ can explain the discrepancy observed in the anomalous magnetic moment of the muon, Δa_μ , while at the same time evading constraints from $Z' \rightarrow \text{invisible}$ at *BABAR* due to the semivisible decays of ν_4 . Finally, a light scalar with $m_{\phi'} \simeq 140$ MeV can explain the KOTO anomaly [126]. Beam dump bounds on such scalars are completely evaded if it decays to long-lived ν_4 states, or are mildly alleviated if it undergoes a dark cascade to e^+e^- within 10 cm, the latter also evading NA62 bounds from $K^+ \rightarrow \pi^+ \cancel{e}$ searches. A correlation between the $|U_{\alpha 4}|^2$ and $|U_{\alpha 5}|^2$ (as well as between $|U_{D4}|^2$ and $|U_{D5}|^2$) neutrino mixing parameters within our three-neutrino model precludes a simultaneous explanation of all of the aforementioned

anomalies without introducing tensions with current experimental bounds. Nevertheless, the signatures we discussed pertain to a far more general class of models, and deserve further consideration due to their unique character.

ACKNOWLEDGMENTS

The authors would like to thank Martin Bauer for interesting discussions regarding the dark photon and $(g-2)_\mu$ phenomenology, and Andrés Olivares-del-Campo and Arsenii Titov for insights on the dark matter models. We acknowledge interesting discussions with Evgueni Goudzovski on the physics potential of NA62. This work was partially supported by Conselho Nacional de Ciência e Tecnologia (CNPq). This project also received support from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie Grant Agreement No. 690575 (RISE InvisiblesPlus) and No. 674896 (ITN Elusives). S. P. and P. B. are supported by the European Research Council under ERC Grant NuMass (FP7-IDEAS-ERC ERC-CG 617143). S. P. acknowledges partial support from the Wolfson Foundation and the Royal Society. The research at the Perimeter Institute is supported in part by the Government of Canada through NSERC and by the Province of Ontario through Ministry of Economic Development and Trade (MEDT).

APPENDIX: KINEMATICS OF EXOTIC KAON DECAYS

In this Appendix we expand on details of the rare kaon decay searches we propose. Beyond the peaks in $m_{\beta\beta} = m_{Z'}$, $m_{p_K-p_\alpha} = m_{\nu_h}$, and $m_{\text{miss}} = 0$, one may explore the correlation and absolute range of two other relevant invariant masses, namely,

$$m_{\alpha\nu}^2 = (p_\mu + p_\nu)^2 = (p_K - p_{\beta^+} - p_{\beta^-})^2, \quad (\text{A1})$$

$$m_{\alpha\beta\beta}^2 = (p_\alpha + p_{\beta^+} + p_{\beta^-})^2. \quad (\text{A2})$$

Their absolute kinematical range is determined, and shown here for the reader's convenience:

$$(m_{\alpha\nu}^2)_{\min}^{\max} = m_K^2 \left[1 + x_{Z'} - \frac{(1 - x_\alpha + x_h)(1 + y) \mp (1 - y)\lambda^{1/2}(1, x_h, x_\alpha)}{2} \right], \quad (\text{A3})$$

$$(m_{\alpha\beta\beta}^2)_{\min}^{\max} = m_K^2 \left[1 - (1 - y) \frac{(1 - x_\alpha + x_h) \mp \lambda^{1/2}(1, x_h, x_\alpha)}{2} \right], \quad (\text{A4})$$

where $\lambda(a, b, c) = (a - b - c)^2 - 4bc$ is the Källén function, $x_{Z'} = (m_{Z'}/m_K)^2$, $x_h = (m_{\nu_h}/m_K)^2$, $x_\alpha = (m_\alpha/m_K)^2$, and $y = (m_{Z'}/m_{\nu_h})^2$.

To illustrate the properties of our signal, we develop our own toy Monte Carlo simulation, and generate 10^4 events

for $K^+ \rightarrow \mu^+(\nu_h \rightarrow \nu(Z' \rightarrow e^+e^-))$ and $K^+ \rightarrow \mu_1^+(\nu_h \rightarrow \nu(Z' \rightarrow \mu_2^+\mu^-))$ decays in a few cases of interest. We fix the kaon momentum to the average value in the NA62 beam, namely, 75 GeV/c. We plot the invariant masses $m_{\nu\alpha}$ and $m_{\alpha\beta\beta}$, as well as the opening angle between the leptons

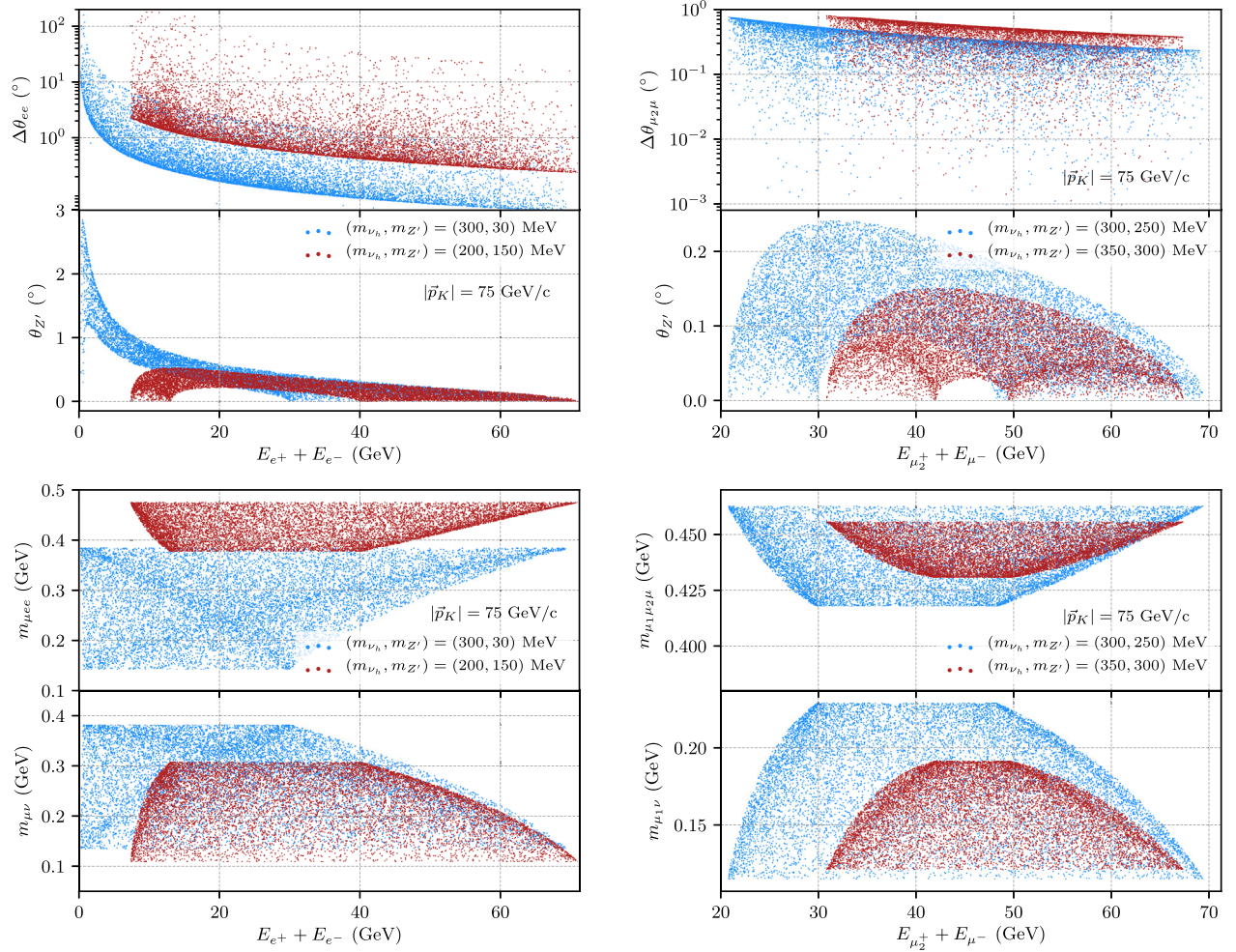


FIG. 4. Kinematics of our $K^+ \rightarrow \mu^+ \nu e^+ e^-$ (left column) and $K^+ \rightarrow \mu_1^+ \nu \mu_2^+ \mu^-$ (right column) events at kaon energies relevant to NA62. We plot 10^4 events in true Monte Carlo variables in each panel. In the top row we show both the separation angle between the decay products of the Z' , $\Delta\theta_{\beta\beta}$, and the angle of the Z' momentum with respect to the kaon beam, $\theta_{Z'}$, both versus the total energy of the decay products of the Z' , $E_{\beta^+} + E_{\beta^-}$. In the bottom row we show the invariant masses $m_{\mu_{(1)}\beta\beta} = \sqrt{(p_{\mu_{(1)}} + p_{\beta} + p_{\beta})^2}$ and $m_{\mu_{(1)}\nu} = \sqrt{(p_{\mu_{(1)}} + p_{\nu})^2}$, also versus the total energy $E_{\beta^+} + E_{\beta^-}$.

$\Delta\theta_{\beta\beta}$, and the angle of the Z' momentum with respect to the kaon beam $\theta_{Z'}$ versus the total Z' energy in Fig. 4. As expected, the kinematics of the signal is highly boosted, with very small angles between the decay products.

Another feature is the broad distributions in invariant masses, except for $m_{\mu_1\mu_2\mu}$, which has somewhat of a smaller range due to the limited phase space of each decay reaction.

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